



+ Addition +



Progression in written calculations

EYFS

Counting songs and reciting number sequences

Counting sets of objects reliably

Finding 1 more (to 20)

Counting on to add 2 single digit numbers



Recording work pictorially



Recording work numerically

$$3 + 2 = 5$$

Key Stage 1

Addition can be done in any order

$$3 + 2 = 2 + 3$$

Encourage children to start with the biggest number

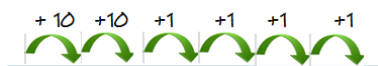
Blank number lines to add 2 single digit numbers.

$$6 + 5 = 11$$



Blank number lines to add 2 digit numbers

$$34 + 24 = 58$$



34 44 54 55 56 57 58

Partitioning into tens and ones

$$\begin{aligned} 42 + 16 &= \\ 40 + 10 &= 50 \\ 2 + 6 &= 8 \\ 50 + 8 &= 58 \end{aligned}$$

Lower Key Stage 2

Partitioning into hundreds, tens and ones

$$249 + 116 = 365$$

$$200 + 100 = 300$$

$$40 + 10 = 50$$

$$9 + 6 = 15$$

$$300 + 50 + 15 = 365$$

Expanded column method

$$86 + 47 =$$

$$\begin{array}{r} 86 \\ + 47 \\ \hline 133 \end{array} \begin{array}{l} (6 + 7) \\ (80 + 40) \end{array}$$

Column method with carrying (up to 4 digit numbers)

$$86 + 47 =$$

$$\begin{array}{r} 86 \\ + 47 \\ \hline 133 \\ \hline 1 \end{array}$$

Upper Key Stage 2

Column method with increasingly larger numbers

$$2457 + 1294 =$$

$$\begin{array}{r} 2457 \\ + 1294 \\ \hline 3751 \\ \hline 11 \end{array}$$

Column method to add decimal numbers

$$159.54 + 64.29 =$$

$$\begin{array}{r} 159.54 \\ + 64.29 \\ \hline 223.83 \\ \hline 111 \end{array}$$



Subtraction



Progression in written calculations

EYFS

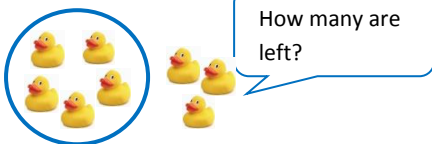
Number rhymes and reciting number sequences

Finding 1 less (to 20)

Counting back to subtract 2 single digit numbers



Removing objects from a group



Recording work pictorially



Recording work numerically

$$5 - 3 = 2$$

Key Stage 1

Counting back in 2s, 5s, 10s (Yr1) and 3s (Yr2) orally and using 100 square.

Removing objects from sets

Finding the difference by counting on

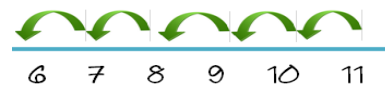
The difference between 11 and 6

$$6 + 5 = 11$$



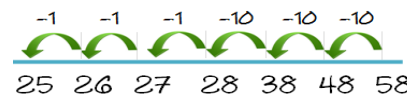
Blank number lines to subtract single digit numbers

$$11 - 5 = 6$$



Blank number lines to subtract 2 digit numbers

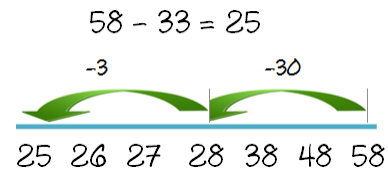
$$58 - 33 = 25$$



Explore the link between inverse operations

Lower Key Stage 2

Blank number lines to subtract 2 digit numbers using larger jumps



Partitioning (practical method using place value counters, working towards written column method)

$$156 - 34$$

$$\begin{array}{r} 100 + 50 + 6 \\ - 30 + 4 \\ \hline 100 + 20 + 2 = 122 \end{array}$$

Column method to subtract 3 and 4 digit numbers

$$\begin{array}{r} 156 - 38 = \\ \begin{array}{r} 1 \quad 5 \quad 6 \\ - \quad 3 \quad 8 \\ \hline 1 \quad 1 \quad 8 \end{array} \end{array}$$

Upper Key Stage 2

Column method to subtract 4 digit numbers

$$2156 - 938 = 1218$$

$$\begin{array}{r} \overset{1}{2} \quad \overset{1}{1} \quad \overset{4}{5} \quad \overset{1}{6} \\ - \quad \quad 9 \quad 3 \quad 8 \\ \hline 1 \quad 2 \quad 1 \quad 8 \end{array}$$

Column method to subtract decimal numbers

$$359.54 + 164.29 = 523.83$$

$$\begin{array}{r} \overset{2}{3} \quad \overset{1}{5} \quad \overset{9}{.} \quad \overset{4}{5} \quad \overset{1}{4} \\ - \quad 1 \quad 6 \quad 4 \quad . \quad 2 \quad 9 \\ \hline 1 \quad 9 \quad 5 \quad . \quad 2 \quad 5 \end{array}$$



✕ Multiplication ✕



Progression in written calculations

EYFS

Songs with counting jumps

(Ants go marching)



Identifying sets of objects which are the same size



Combining sets of objects which are the same size

$$\boxed{3} + \boxed{3} + \boxed{3} = 9$$

Grouping objects into 2s and 10s

Counting in 2s, 5s and 10s

Doubling using objects

Key Stage 1

Practical methods leading to pictorial recording (Ponds and Fish)



$$3 \times 3 = 9$$

Dot Arrays

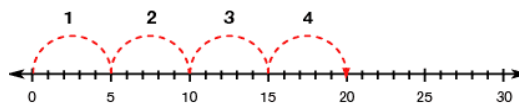


factor factor product

$$3 \times 6 = 18$$

number of groups number in each group number in all

Number Lines



factor 4 x factor 5 = product 20

Multiplication can be done in any order

$$3 \times 6 = 6 \times 3$$

Times Tables

Year 2 children should know their 2, 5 and 10 times tables.

Lower Key Stage 2

Grid Method (as a step towards formal written methods)

$$35 \times 7 = 245$$

X	30	5
7	210	35
		210 + 35 = 245

Short Multiplication

24 x 6 becomes

$$\begin{array}{r} 24 \\ \times 6 \\ \hline 144 \end{array}$$

Answer: 144

Times Tables

Year 3 children should know their 2, 3, 4, 5, 8 and 10 times tables

Year 4 children should know all their tables up to and including 12 x 12.

Upper Key Stage 2

Short multiplication for 2, 3 and 4 digit by 1 digit multiplication

2741 x 6 becomes

$$\begin{array}{r} 2741 \\ \times 6 \\ \hline 16446 \\ 42 \\ \hline \end{array}$$

Answer: 16 446

Long multiplication for 2 and 3 digits by 2 digit numbers

124 x 26 becomes

$$\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 2480 \\ \hline 3224 \\ 11 \\ \hline \end{array}$$

Answer: 3224



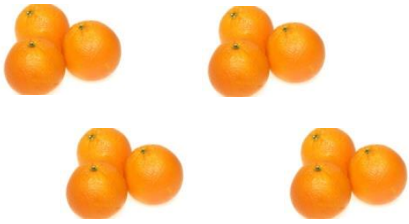
÷ Division ÷



Progression in written calculations

EYFS

Sharing objects fairly between groups of children.

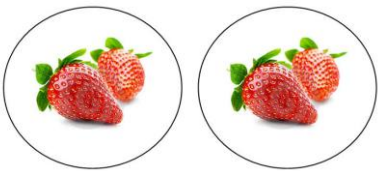


Cutting objects in half. How many pieces



Counting backwards in 2s and 10s

Halving groups of objects



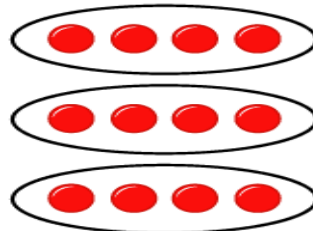
Key Stage 1

Practical methods leading to pictorial recording (Ponds and Fish)



$$9 \div 3 = 3$$

Dot Arrays

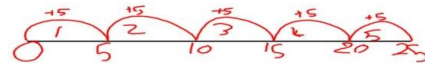


$$12 \div 4 = 3$$

Number Lines

(How many 5s are in 25?)

$$25 \div 5 = 5$$



Explore links between inverse operations

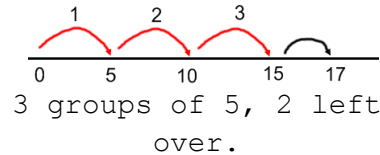
Times Tables

Year 2 children should know the division facts for the 2, 5 and 10 times tables.

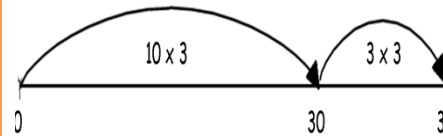
Lower Key Stage 2

Number Lines (With remainders)

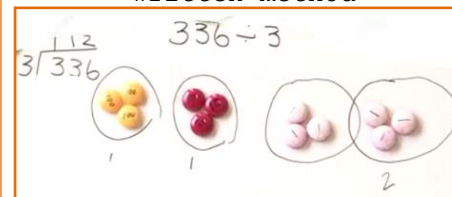
$$17 \div 5 = 3 \text{ r} 2$$



Chunking on a number line:



Progressing to standard written method



Times Tables

Year 3 should know division facts for the 2, 3, 4, 5, 8 & 10 times tables

Year 4 should know division facts for all tables to 12 x12.

Upper Key Stage 2

Standard written method with remainders.



Long Division for up to 4 digit numbers by 2 digit numbers.

Long division				
432 ÷ 15 becomes				
		2	8	r 12
1	5	4	3	2
		3	0	0
		1	3	2
		1	2	0
		1	2	

Short Division for up to 4 digit numbers by 2 digit numbers.

496 ÷ 11 becomes				
		4	5	r 1
1	1	4	9	6
		4	5	
		1	1	
		Answer: 45 $\frac{1}{11}$		

Prime Numbers

Identify prime numbers, common factors and common multiples.